

The class algorithm stops when  $\frac{b_i - a_i}{2} < \epsilon = \text{tolerance}$ .

Other stopping methods commonly used:

$$(1) |p_i - p_{i+1}| < \epsilon.$$

Problem: there are cases where  $p_i - p_{i+1} \rightarrow 0$ , but  $\{p_i\}$  diverges.

$$\text{Example: } p_i = \sum_{n=1}^i \frac{1}{n}$$

$$(2) |f(p_i)| < \epsilon$$

Problem:  $p_i$  might not be near  $p$ .

$$(3) \frac{|p_i - p_{i+1}|}{|p_i|} < \epsilon.$$

Usually the best without other information.

**EXAMPLE.** Find the solution of  $2 + \cos(e^x - 2) - e^x = 0$  on  $[0.5, 1.5]$  to within  $10^{-3}$ .

$$\frac{b - a}{2^n} < 10^{-3} \iff \frac{1}{2^n} < 10^{-3} \iff 2^n > 1000 \iff n > \log_2 1000 \approx 9.97.$$

Thus 10 is an upper bound on the number of iterations necessary to give us the accuracy required.