

```
[ >
```

Normal and t Distributions

```
[ > restart;
```

```
> with(plots);
```

```
Warning, the name changecoords has been redefined
```

```
[animate, animate3d, animatecurve, changecoords, complexplot, complexplot3d, conformal,
  contourplot, contourplot3d, coordplot, coordplot3d, cylinderplot, densityplot, display, display3d,
  fieldplot, fieldplot3d, gradplot, gradplot3d, implicitplot, implicitplot3d, inequal, listcontplot,
  listcontplot3d, listdensityplot, listplot, listplot3d, loglogplot, logplot, matrixplot, odeplot, pareto,
  pointplot, pointplot3d, polarplot, polygonplot, polygonplot3d, polyhedra_supported,
  polyhedraplot, replot, rootlocus, semilogplot, setoptions, setoptions3d, spacecurve,
  sparsematrixplot, sphereplot, surfdata, textplot, textplot3d, tubeplot]
```

```
> with(stats);
```

```
[anova, describe, fit, importdata, random, statevalf, statplots, transform]
```

```
> with(statevalf);
```

```
[cdf, dcdf, icdf, idcdf, pdf, pf]
```

```
> with(pdf);
```

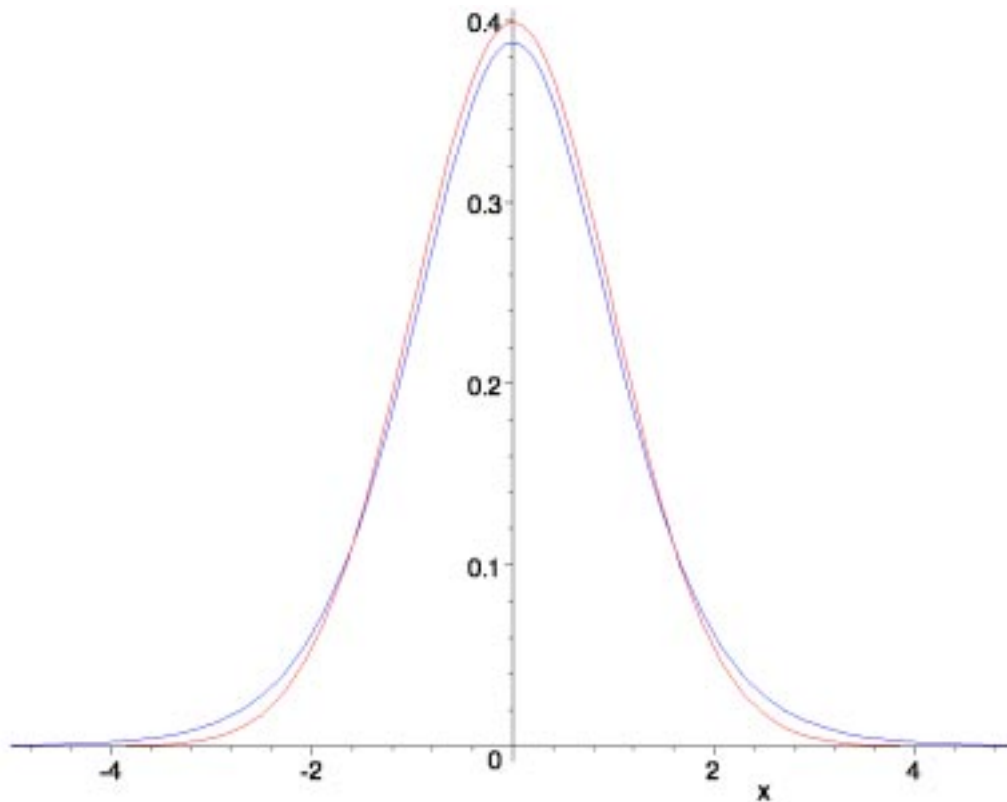
```
[ $\beta$ , cauchy, chisquare, exponential, fratio,  $\gamma$ , laplaced, logistic, lognormal, normald, studentst,
  uniform, weibull]
```

```
[We first wish to compare the normal distribution (red) with the  $t$  distribution with 9 degrees of
freedom (blue).
```

```
> p0:=plot(normald(x),x=-5..5,color=red):
```

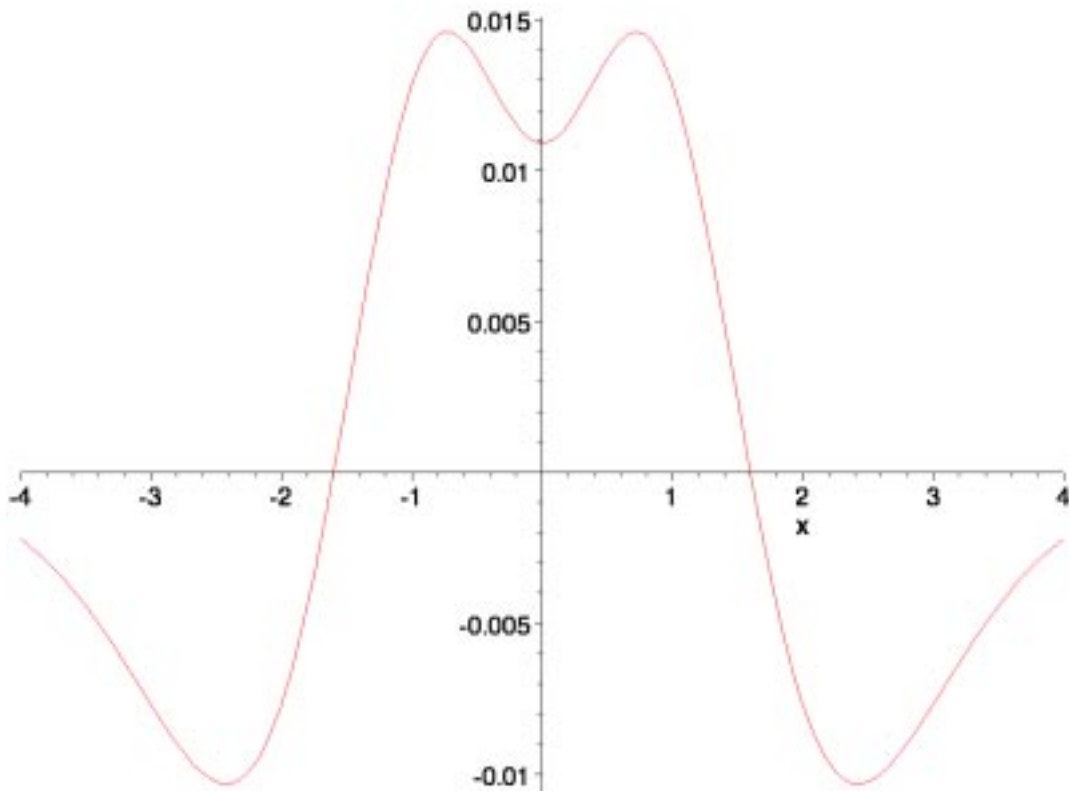
```
p1:=plot(studentst[9](x),x=-5..5,color=blue):
```

```
display(p0,p1);
```



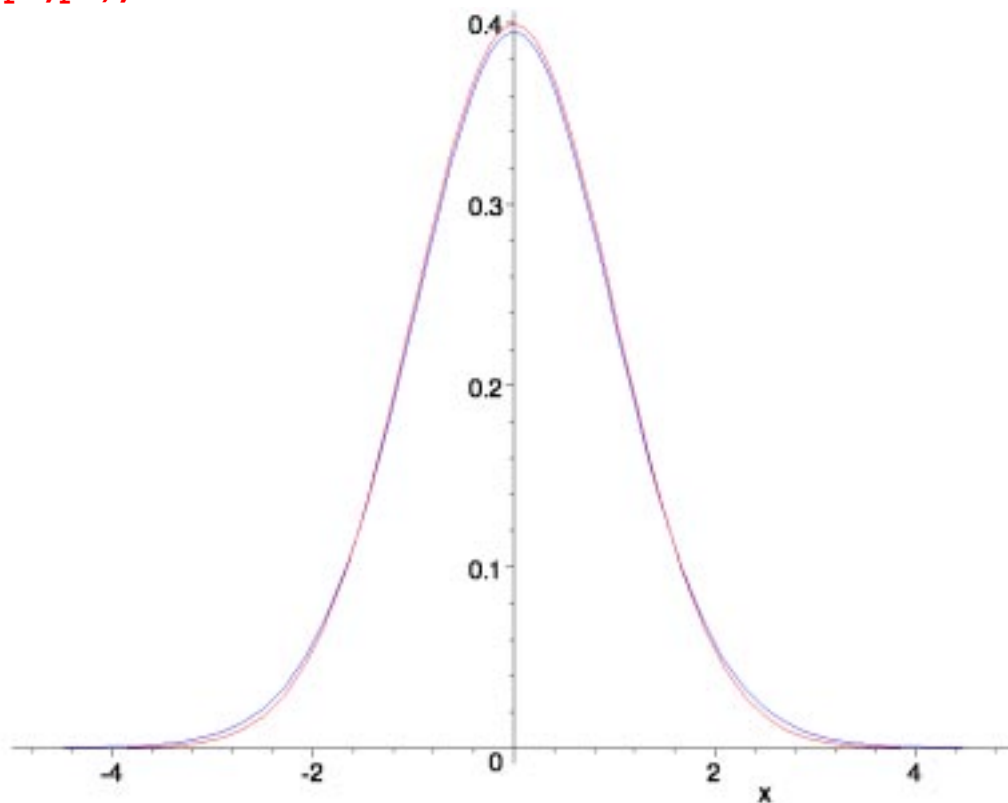
We see the normal curve is higher in the middle but lower on the extremes. Let's compute the difference of the curves.

```
> plot(normald(x)-studentst[9](x),x=-4..4);
```



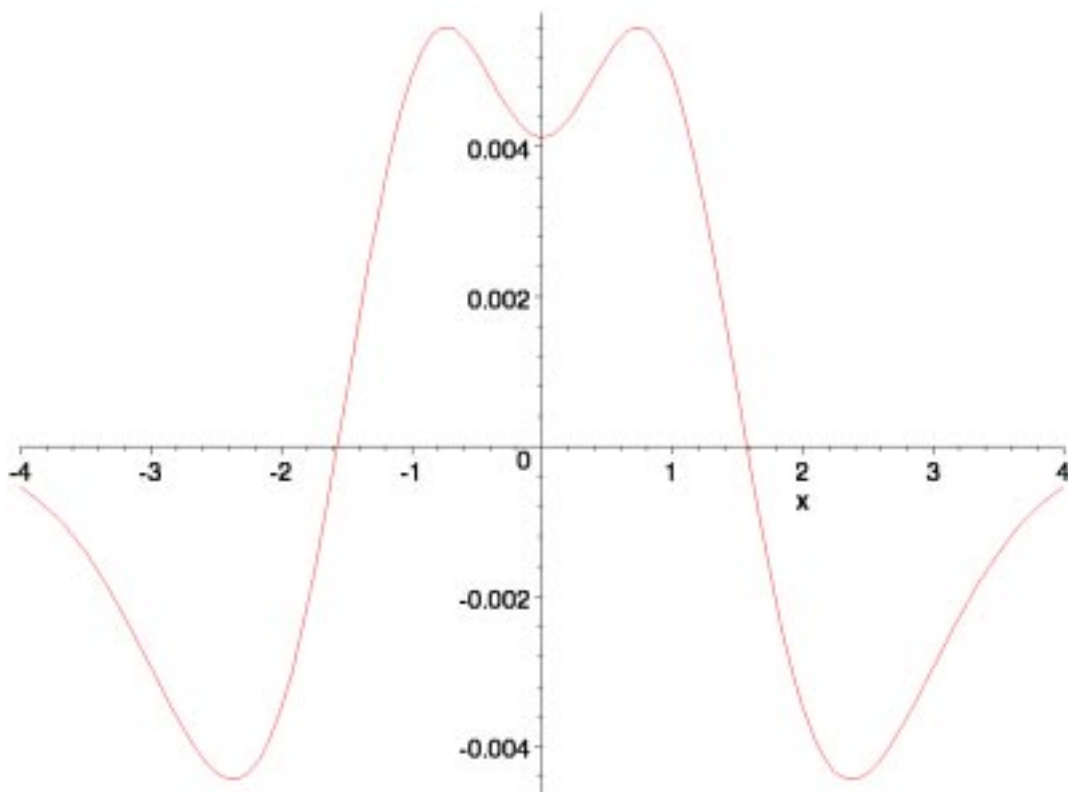
Next let's compare the normal distribution (red) with the t distribution with 24 degrees of freedom (blue), which we would often use when $n = 25$.

```
p0:=plot(normald(x),x=-5..5,color=red):  
p2:=plot(studentst[24](x),x=-5..5,color=blue):  
display(p0,p2);
```



We have the same relationship as before, but the curves are much closer. Let's again compute the difference of the curves.

```
> plot(normald(x)-studentst[24](x),x=-4..4);
```



With this small difference, you can see why we often, for convenience sake, use z instead of t for large populations (when n is greater than or equal to 25). What is the total accumulated absolute error in using t instead of z when $n = 25$?

```
> dif:=abs(normald(x)-studentst[24](x));
      dif:=|normald(x) - studentst24(x)|
> int(dif,x=-infinity..infinity);
      ∫-∞∞ |normald(x) - studentst24(x)| dx
> evalf(%);
      .02618338748
```

This is pretty small. Let's see what happens when $n = 30$.

```
> dif:=abs(normald(x)-studentst[29](x));
      dif:=|-normald(x) + studentst29(x)|
> int(dif,x=-infinity..infinity);
      ∫-∞∞ |-normald(x) + studentst29(x)| dx
> evalf(%);
      .02169647044
```

This total accumulated absolute error will keep getting smaller as n increases.

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